

## Handout 7: Problem Set 7

*Instructor: John Hopcroft**Teaching Assistant: Zhengyang Liu, Tao Xiao***Due by Wednesday, Dec 27th, 4pm.**

- 1 Define a valid computation of a turing machine so that it can be expressed as the intersection of two context-free language. Then using  $L = \{w_i \vdash w_{i+1} \mid w_i \text{ and } w_{i+1} \text{ are ID where } w_i \vdash w_{i+1} \text{ in one step of the turing machine}\}$ . Construct  $L_1$  and  $L_2$  so that  $L_1 \cap L_2$  is the set of valid computation.
- 2 Construct a cfg for  $\{w_i \vdash w_{i+1}^R\}$ .
- 3 Construct turing machine that multiplies, that is  $q_0|0^n|0^m \vdash^* q|0^n|0^m|0^{nm}$ .