

《复分析》课程教学大纲

Course Outline

课程基本信息 (Course Information)					
课程代码 (Course Code)	MA214	*学时 (Credit Hours)	64	*学分 (Credits)	4
*课程名称 (Course Title)	(中文) 复分析				
	(英文) Complex Analysis				
*课程性质 (Course Type)	专业基础课				
授课对象 (Target Audience)					
*授课语言 (Language of Instruction)	中英双语				
*开课院系 (School)	致远学院/数学科学学院				
先修课程 (Prerequisite)	数学分析				
授课教师 (Instructor)	戎锋	课程网址 (Course Webpage)			
*课程简介 (Description)	<p>本课程主要学习单复变函数相关理论。课程强调最基本的思想和严格的证明。希望学生能从分析、代数、几何等多个角度来理解经典的复分析。先修的数学分析课程对本课程至关重要，如学生能有代数和几何方面的一些知识储备则更佳。课程学习的主要内容包括：复数、复解析函数、最大模原理、Cauchy 定理、Liouville 定理、级数、孤立奇点、留数、Rouche 定理、Schwarz 引理、Poisson 积分、Riemann 映照定理等。</p>				
*课程简介 (Description)	<p>This course is an introduction to the theory of complex valued functions of a complex variable. Fundamental ideas and rigorous proofs will be emphasized. Students are expected to understand the classical theory of complex analysis from the <i>analytic</i>, <i>algebraic</i> and <i>geometric</i> point of view. The prerequisite of a course in mathematical analysis is essential. Some background in algebra and geometry is preferred. Topics to be covered include (but not limited to): complex numbers, analytic functions, maximum principle, Cauchy's theorem, Liouville's theorem, power series, isolated singularities, residues, Rouche's theorem, Schwarz lemma, Poisson integral and the Riemann mapping theorem.</p>				

课程教学大纲 (course syllabus)

*学习目标(Learning Outcomes)

1. The definition of complex numbers; plus some topology, algebra and geometry
2. Some basic complex analytic functions; power series
3. The Cauchy-Riemann equation and its consequences
4. Complex line integrals; Cauchy integral formula
5. Entire functions; Liouville theorem
6. Mean-value property; Maximum principle; Morera theorem; Goursat theorem, etc.
7. Multi-valued analytic functions and the associated Riemann surfaces
8. Isolated singularities; The Laurent decomposition
9. Residue theorem and using it to compute various integrals
10. The argument principle; Rouché theorem; Hurwitz theorem, winding numbers, etc.
11. Examples of conformal mappings; The Schwarz lemma
12. Riemann mapping theorem
13. Properties of harmonic functions; Poisson integral
14. Infinite products; analytic continuation; Gamma function; Zeta function, etc.
15. Some selected more advanced topics

*教学内容、进度安排及要求
(Class Schedule & Requirements)

教学内容	学时
Complex numbers	4
Examples of analytic functions; Power series	4
Cauchy-Riemann equation and other properties of analytic functions	4
Complex line integral	4
Entire functions; Liouville theorem	4
Further properties of analytic functions	4
Multi-valued analytic functions; Riemann surfaces	4
Isolated singularities	4
Midterm; Residue theorem	4
Residue calculus	4
Logarithmic integral; Argument principle	4
Conformal mappings; Schwarz lemma	4
Riemann mapping theorem	4
Harmonic functions	4

	Gamma function; Zeta function	4
	Some further topics; Review	4
*考核方式 (Grading)	(成绩构成) [暂定] 20% - 平时成绩 Homework; 35% - 期中成绩 Midterm; 45% - 期末成绩 Final	
*教材或参考资料 (Textbooks & Other Materials)	Textbook: "Complex Analysis" , by J. Bak and D.J. Newman References: "Complex Analysis" , by L. Ahlfors "Complex Analysis" , by T.W. Gamelin "Complex Analysis" , by E.M. Stein and R. Shakarchi	
其它 (More)		
备注 (Notes)		

备注说明:

1. 带*内容为必填项。
2. 课程简介字数为 300-500 字; 课程大纲以表述清楚教学安排为宜, 字数不限。